

Roulette Inflation hep-th/0612197

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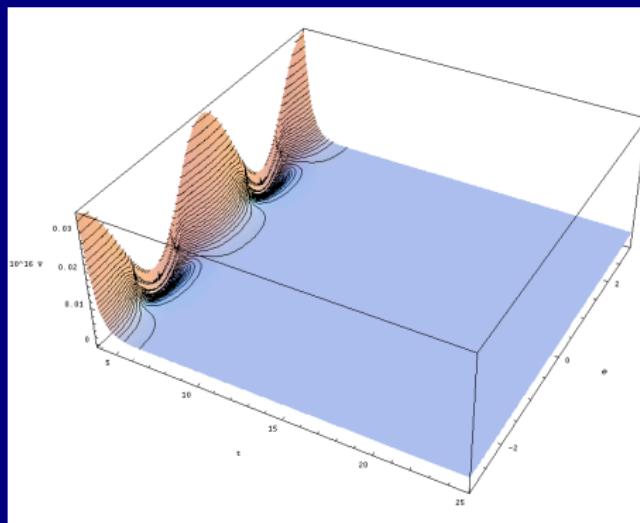


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Introduction



- $W = W_0 + \sum_i A_i e^{-a_i T_i}, \quad T_i = \tau_i + i\theta_i$
- $K = -2 \ln(\mathcal{V} + \frac{\xi}{2}), \quad \mathcal{V} = \alpha \left(\tau_1^{3/2} - \sum_{i=2}^n \lambda_i \tau_i^{3/2} \right)$

SUGRA

$$V = e^K \left(K^{i\bar{j}} D_i W D_{\bar{j}} \bar{W} - 3|W|^2 \right)$$

- $D_i = \partial_i + K_i$, $K_i = \frac{\partial K}{\partial T^i}$, $K_{i\bar{j}} = \frac{\partial^2 K}{\partial T^i \partial \bar{T}^j}$
- pen and paper
- # terms $\propto (\# \text{fields})^2$
- \Rightarrow Mathematica: $\approx 1 \text{ min}$ for 3 fields
- Here: 3 complex fields $(T_1, T_2) \Leftrightarrow (V, T_2)$

⇒ Resulting potential

$$\begin{aligned}
 V(T_1, \dots, T_n) = & \\
 & \frac{12W_0^2\xi}{(4\mathcal{V} - \xi)(2\mathcal{V} + \xi)^2} + \sum_{i=2}^n \frac{12e^{-2a_i\tau_i}\xi A_i^2}{(4\mathcal{V} - \xi)(2\mathcal{V} + \xi)^2} + \frac{16(a_i A_i)^2 \sqrt{\tau_i} e^{-2a_i\tau_i}}{3\alpha\lambda_2(2\mathcal{V} + \xi)} \\
 & + \frac{32e^{-2a_i\tau_i} a_i A_i^2 \tau_i (1 + a_i \tau_i)}{(4\mathcal{V} - \xi)(2\mathcal{V} + \xi)} + \frac{8W_0 A_i e^{-a_i\tau_i} \cos(a_i\theta_i)}{(4\mathcal{V} - \xi)(2\mathcal{V} + \xi)} \left(\frac{3\xi}{(2\mathcal{V} + \xi)} + 4a_i\tau_i \right) \\
 & + \sum_{\substack{i,j=2 \\ i < j}}^n \frac{A_i A_j \cos(a_i\theta_i - a_j\theta_j)}{(4\mathcal{V} - \xi)(2\mathcal{V} + \xi)^2} e^{-(a_i\tau_i + a_j\tau_j)} [32(2\mathcal{V} + \xi)(a_i\tau_i + a_j\tau_j \\
 & + 2a_i a_j \tau_i \tau_j) + 24\xi]
 \end{aligned}$$

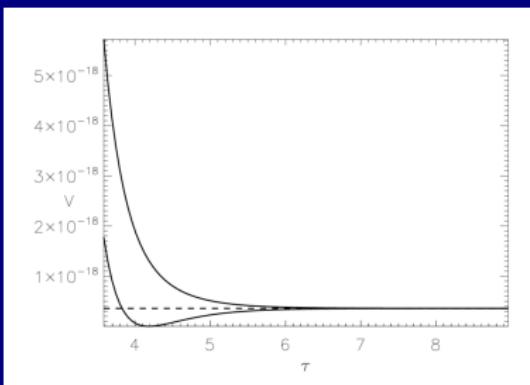
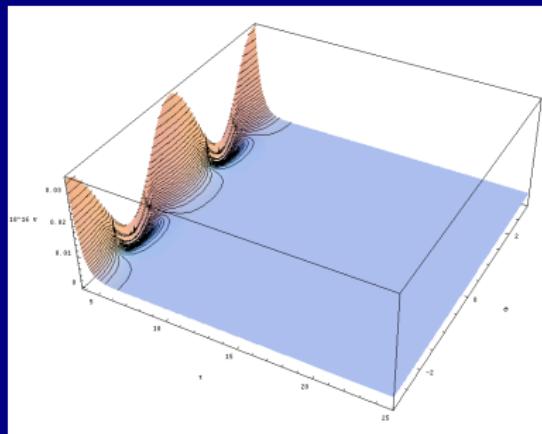
Stabilization and Uplift

- inflaton T_2
- \mathcal{V} stabilized by extra fields $T_3 \dots T_n$: $\sum_{i=2}^n \frac{\lambda_i}{a_i^{3/2}} \gg \frac{\lambda_2}{a_2^{3/2}}$
- assume $V = V(\mathcal{V}, T_3, \beta)$
- $V_m < 0$
 - Need uplift $V_{\text{up}} = \frac{\beta}{\mathcal{V}^\alpha}$
 - self-consistent uplift procedure:

$$\text{solve } \left\{ \begin{array}{l} V(\mathcal{V}, T_3, \beta) = \min \\ V(\mathcal{V}, T_3, \beta) = 0 \end{array} \right\} \Rightarrow V(T_2) \equiv V(\mathcal{V}_m, T_{3,m}, \beta, T_2)$$
- inflaton $T_2 \equiv \tau + i\theta$

$$V(\tau, \theta) = \frac{8(a_2 A_2)^2 \sqrt{\tau} e^{-2a_2 \tau}}{3\alpha \lambda_2 \mathcal{V}_m} - \frac{4W_0 a_2 A_2 \tau e^{-a_2 \tau} \cos(a_2 \theta)}{\mathcal{V}_m^2} + \Delta V$$

Form of the potential

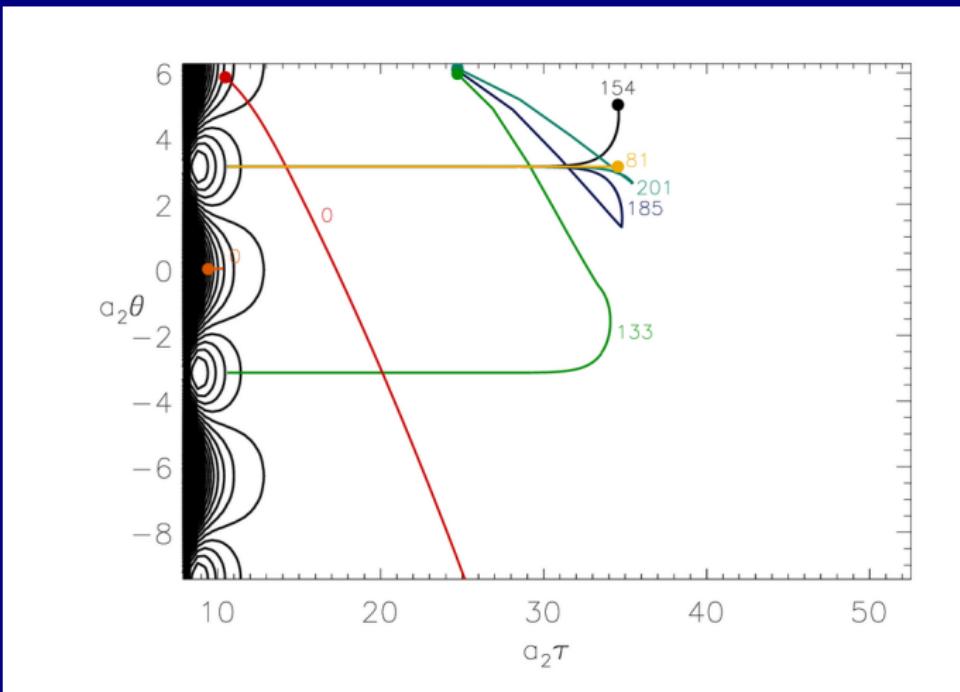


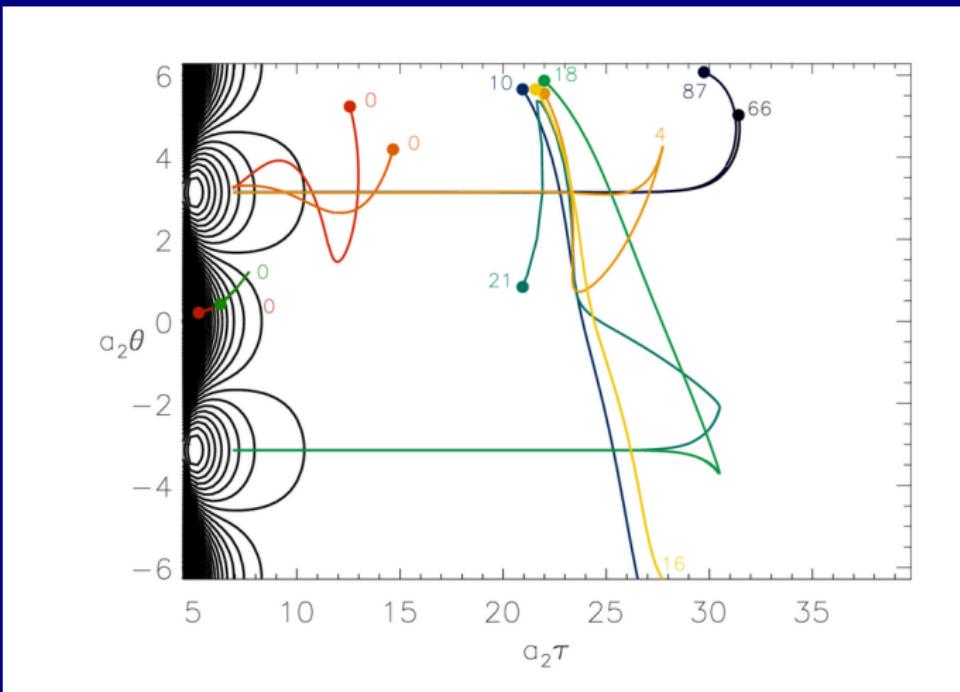
Equations of Motion

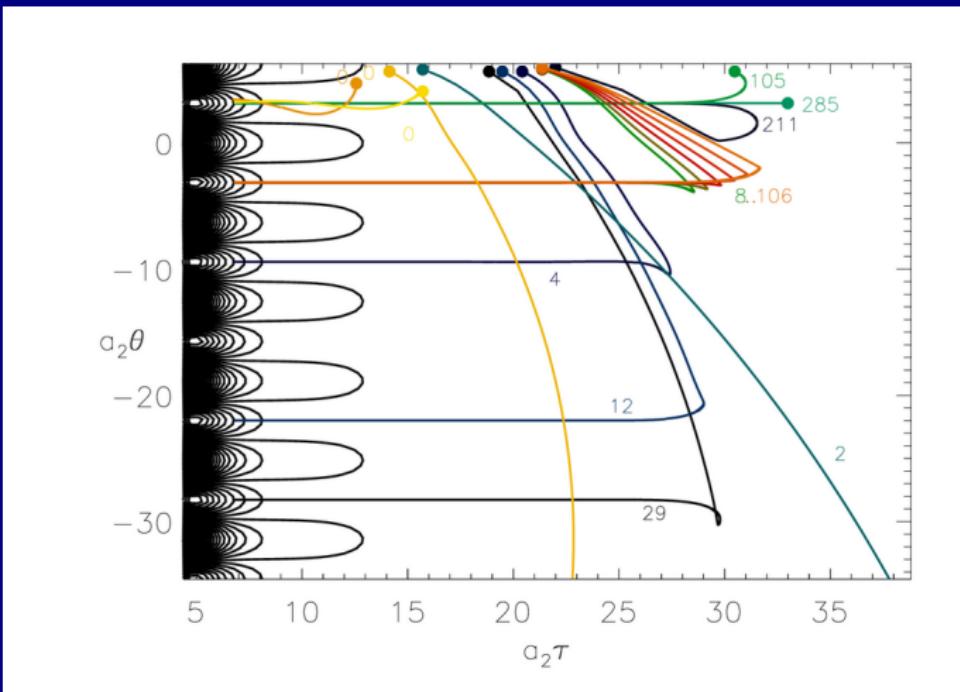
Parameter	W_0	a_2	A_2	λ_2	α	ξ	g_s	\mathcal{V}	$\Delta\varphi/M_p$
Parameter set 1	300	$2\pi/3$	0.1	1	$1/9\sqrt{2}$	0.5	1/10	10^6	2×10^{-3}
Parameter set 2	6×10^4	$2\pi/30$	0.1	1	$1/9\sqrt{2}$	0.5	1/10	10^8	1×10^{-3}
Parameter set 3	4×10^5	$\pi/100$	1	1	$1/9\sqrt{2}$	0.5	1/10	10^9	1.4×10^{-3}
Parameter set 4	200	π	0.1	1	$1/9\sqrt{2}$	0.5	1/10	10^6	1.5×10^{-3}
Parameter set 5	100	$2\pi/3$	0.1	1	$1/9\sqrt{2}$	0.5	1/10	10^6	1.9×10^{-3}
Parameter set 6	75	$2\pi/6$	1	1	$1/9\sqrt{2}$	0.5	1/10	10^8	4×10^{-4}

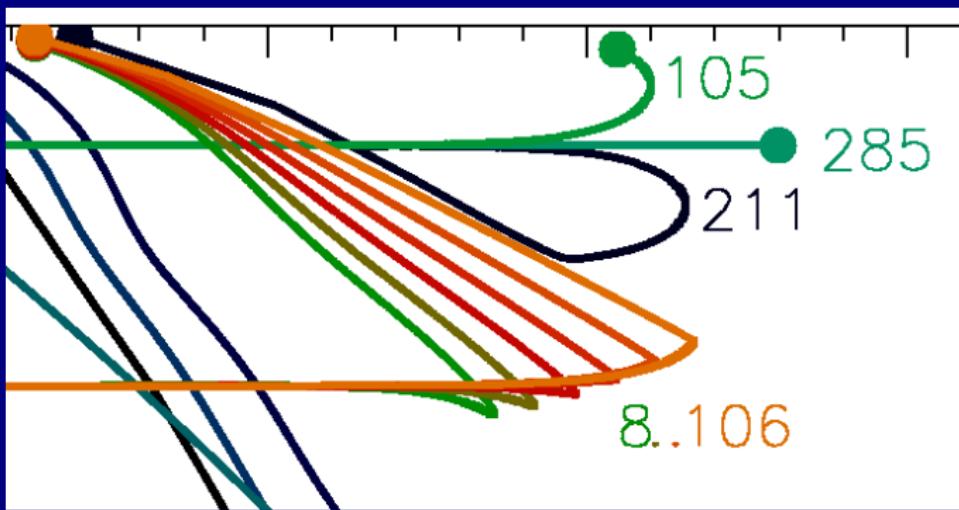
Solve until $\epsilon = 1$:

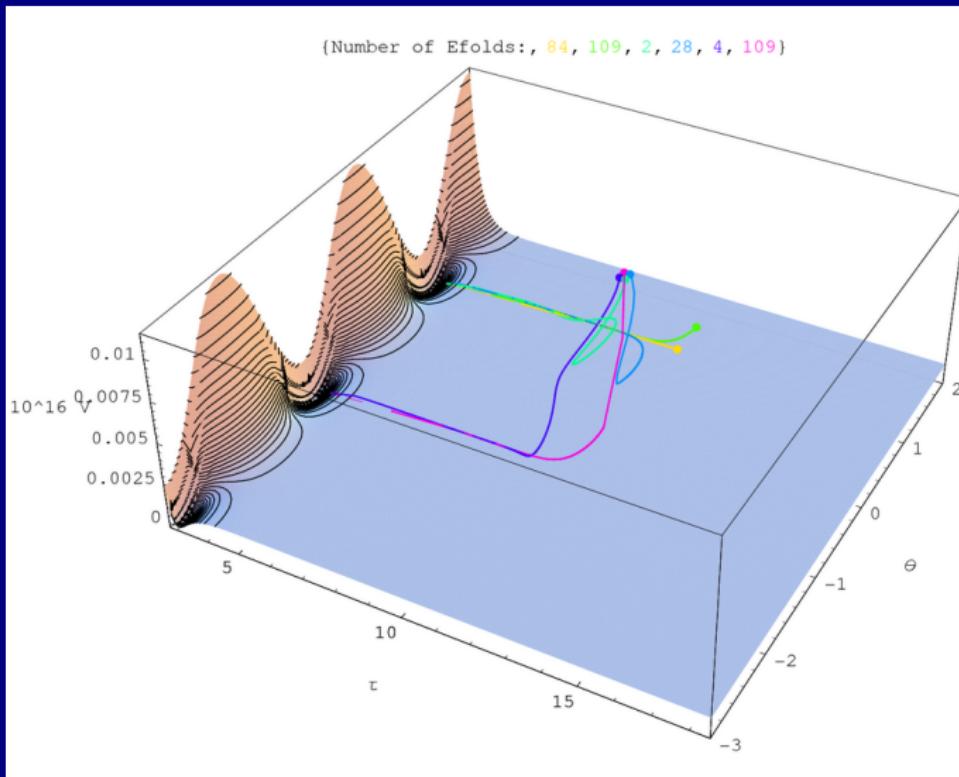
$$\begin{aligned}
 \dot{\phi}^i &= \frac{1}{2a^3} G^{ij} P_j, \\
 \dot{P}_i &= -\frac{1}{4a^3} \frac{\partial G^{kl}}{\partial \phi^i} P_k P_l - a^3 \frac{\partial V}{\partial \phi^i}, \\
 \dot{a} &= aH, \\
 \dot{H} &= -\frac{1}{4a^3} G^{ij} P_i P_j,
 \end{aligned}$$









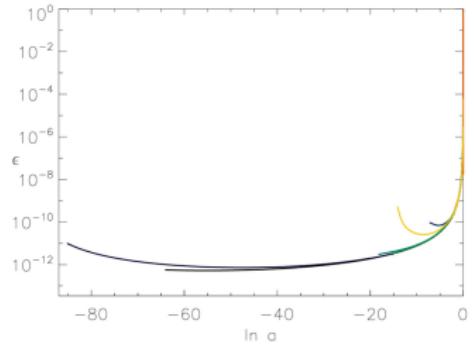
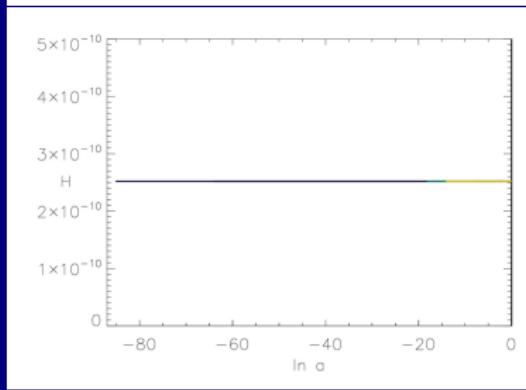
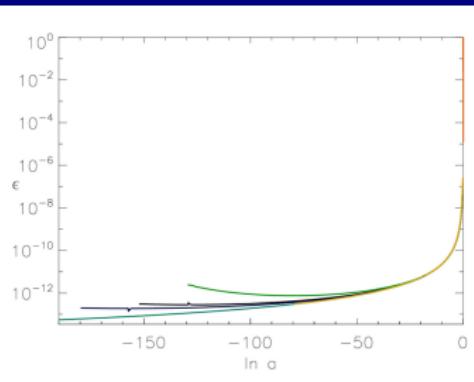
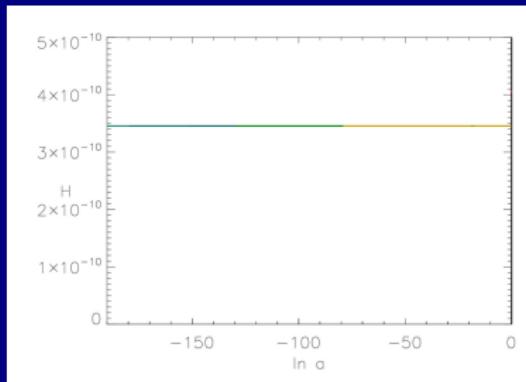


Features

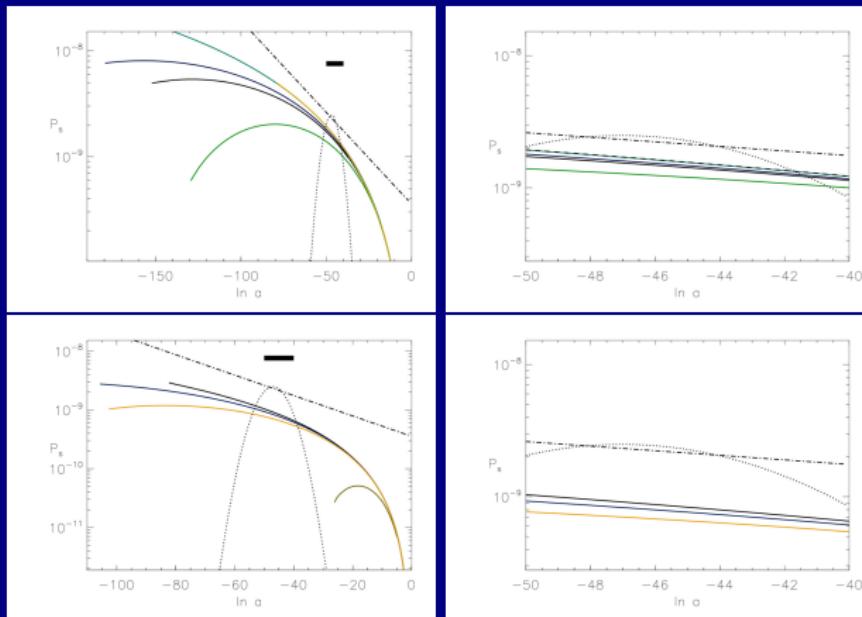
- axionic direction
- dependence on initial conditions
- bifurcation points
- lots of efolds
- isocurvature perturbations
- $N = 40 \dots 50$

(from $N(k) = 62 - \ln \frac{k}{6.96 \times 10^{-5} \text{ Mpc}^{-1}} + \Delta$, with $\Delta = -\ln \frac{10^{16} \text{ GeV}}{V_k^{1/4}} + \frac{1}{4} \ln \frac{V_k}{V_{\text{end}}} - \frac{1}{3} \ln \frac{V_{\text{end}}}{\rho_{\text{reh}}^{1/4}}$)

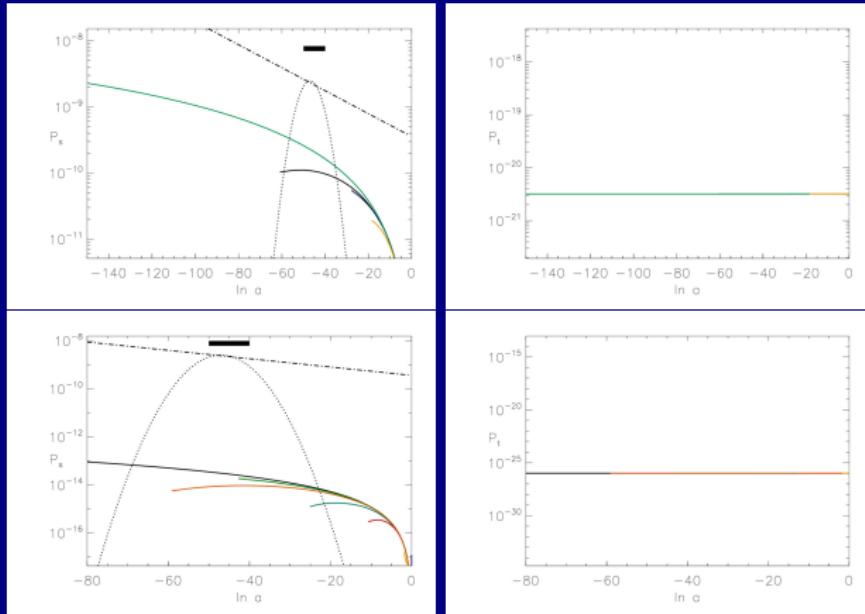
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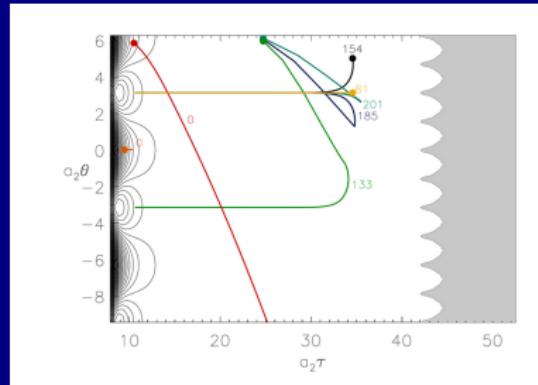
Template $P_S \propto k^{n_s-1}$ with
 a) dash-dot: $n_s = 0.95, n_{\text{run}} = 0$
 b) dotted: $n_s = 0.95, n_{\text{run}} = -0.055$, pivot point $N = 45$



Parameter sets with wrong amplitude of fluctuation

Initial conditions

- Stabilization from 3rd ... n^{th} field $T_3 \dots T_n$
- \Rightarrow uniform (?) distribution of initial values of (τ, θ)
- maybe existence of region of eternal inflation? \Rightarrow YES!



Conclusions

- rich structure
 - axionic direction
 - bifurcation points
 - lots of efolds
- stochastic regime